

The extended Hückel theory: - The HMO theory is applicable to planar conjugated π -systems only. An extension to this empirical method was made by Hoffmann in which both σ and π e⁻s are considered and can be applicable to both planar and non planar molecules. This is known as EHT.

Both HMO and EH methods begin with the approximation that the complete Hamiltonian is a sum of i.e. Hamiltonians; $\hat{H} = \sum_i \hat{H}(i)$. But Hamiltonian is not specified \Rightarrow Schrodinger eqⁿ is not solved.

The complete electronic wave function Ψ is a simple product of i.e. wave functions ψ_i and total energy E is the sum of i.e. molecular orbital energies E_i .

The molecular orbitals are linear combination of atomic orbitals ϕ_r containing valence e⁻s only.

$$\Psi_i = \sum_r a_{ir} \phi_r$$

The atomic orbitals are of Slater type (STO). Linear variation method leads to secular eqⁿ

$$\sum [a_{ir} (H_{rs} - E_i S_{rs})] = 0$$

The secular determinant,

$$\det | H_{rs} - E_i S_{rs} | = 0$$

where $H_{rs} = \int \phi_r \hat{H}(i) \phi_s dt$

$$S_{rs} = \int \phi_r \phi_s dt$$

and $E_i =$ Energy of the mo Ψ_i

All this is similar to HMO theory. The diff lies in that now all valence atomic orbitals will be taken into the linear combination; in addition

all overlap integrals are evaluated. formulas for which are readily available

The diagonal elements, $H_{rr} = \int \phi_r \hat{H}(i) \phi_r d\tau$
 H_{rr} = average energy of an e^- in the AO ϕ_r centred on the atom r in the molecule.

- H_{rr} = orbital energy of AO,
- ϕ_r = Ionization potential of the atom in its valence state (with opposite sign)

The off diagonal element $H_{rs} \Rightarrow$

$$H_{rs} = \frac{1}{2} K S_{rs} (H_{rr} + H_{ss}) \text{ Approximate formula}$$

whose K = Adjusted b/w 1 & 3

- H_{rr} and H_{ss} are $-ve \Rightarrow H_{rs} = -ve$ if S_{rs} is $+ve$

If $S_{rs} = 0 \Rightarrow H_{rs} = 0$

- air are obtained by substituting H_{rs} and S_{rs}

Total energy, $E = \sum E(i)$

from MOs, Ψ ; known the electronic wave function

Ψ is written as the Slater determinant.